POINT BACH

 $X = \pm \sqrt{4 - y} \quad \times = -\frac{1}{3}y$ If the region is revolved around the line x = -6, [a]

write, BUT DO NOT EVALUATE, an integral (or sum of integrals) for the volume of the solid

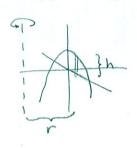
[i] using the disk or washer method (NOTE: You do NOT need to simplify your integrand.)



$$\frac{77}{12} \int_{-12}^{3} ((\sqrt{4-y}+6)^{2} - (-\frac{1}{3}y+6)^{2}) dy + \frac{1}{3} ((\sqrt{4-y}+6)^{2} - (-\sqrt{4-y}+6)^{2}) dy$$

$$4-x^{2}=-3x$$
 $0=x^{2}-3x-4$
 $0=(x-4)(x+1)$
 $x=-1,4$
 $y=3$
 $y=-12$

using the shell method (NOTE: You do NOT need to simplify your integrand.) [ii]

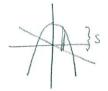


$$2\pi \int_{-1}^{4} (x+6)(4-x^2+3x) dx$$

Suppose the region is the base of a solid. Cross sections perpendicular to the x – axis are isosceles right triangles with one leg in the [b] base. Write, BUT DO NOT EVALUATE, an integral (or sum of integrals) for the volume of the solid.



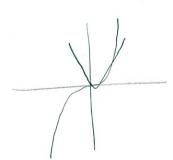
$$\frac{1}{2}\int_{-1}^{4}(4-x^2+3x)^2dx$$



Find the area bounded by the curves $y = 4x^3$ and $y = 16x^2 - 12x$.

$$4x^3 = 16x^2 - 12x$$

 $4x^3 - 16x^2 + 12x = 0$
 $4x(x^2 - 4x + 3) = 0$



$$O\int_{0}^{1} (4x^{3} - (16x^{2} - 12x)) dx + \int_{1}^{3} (16x^{2} - 12x - 4x^{3}) dx$$

$$= \left(X^{4} - \frac{15}{3} x^{3} + 6 x^{2} \right) \Big|_{0}^{1} + \left(-x^{4} + \frac{15}{3} x^{3} - 6 x^{2} \right) \Big|_{1}^{3}$$

SCORE:

/8 PTS

$$= 7 - 5\frac{1}{3} + 9 + 7 - 5\frac{1}{3}$$

The region bounded by $y = x^2 - 9$, y = 2(x - 5) and y = 0 is revolved around the line y = 10.

SCORE: ____/8 PTS

Write, BUT DO NOT EVALUATE, an integral (or sum of integrals) for the volume of the solid using as few integrals as possible.

$$x^{2}-9=2x-10$$

 $x^{2}-2x+1=0,0$
 $x=1 \rightarrow y=-8$

